

***Please show all of your work so that we have the option of giving you partial credit for your work. Please circle your final answers. Make a copy of your calculations and answers so you will be able to check your answers when the answer key is posted on the class website after the testing period has ended. Please use Blue Books provided.***

1. A sleep researcher conducts an experiment to determine if sleep loss affects ability to maintain sustained attention. Fifteen subjects are randomly assigned to the following three groups of 5 subjects each: group 1, which gets the normal amount of sleep (7-8 hours), group 2, which is sleep-deprived for 24 hours; and group 3, which is sleep-deprived for 48 hours. All three groups are tested on the same auditory vigilance task. Subjects are presented with half-second tones spaced at irregular intervals over a 30-minute duration. Occasionally, one of the tones is slightly shorter than the rest. The subject's task is to detect the shorter tones. Ten shorter tones were presented. The following table indicates the number of shorter tones correctly detected (a higher score means better performance).

Normal Sleep	Sleep-Deprived for 24 hours	Sleep-Deprived for 48 hours
10	5	5
9	4	2
8	3	1
7	4	2
8	7	3

- a. State the scientific hypothesis and the PCH (plausible competing hypothesis) of chance (5 points).
- b. Translate the scientific hypothesis and the PCH of chance to statistical hypotheses – that is state  $H_0$  and  $H_1$  (2 points).
- c. Name the test statistic you will use to decide between the statistical hypotheses (5 points).
- d. Does the issue of one-tailed versus two-tailed statistical hypotheses apply to this test? (yes/no) (2 points).
- e. What is the alpha level (level of significance or p-value) you will use? (2 points).
- 1f. Calculate the degrees of freedom (df) you will use for your critical value (or values) (4 points).
- 1g. What is the critical value (or values)? (2 points).

1h. Draw a line representing the range of your statistic. What is the value predicted by  $H_0$ ? Draw it on the line. Also draw the critical value (or values) on the line. Label the “Reject  $H_0$ ” region (or regions). Label the “Do not Reject  $H_0$ ” region. (5 points).

1i. Find the means of the three groups and graph them (5 points).

1j. Does the pattern of the data fit the scientific hypothesis? Why or why not? (2 points).

1k. Calculate the value of your test statistic from the data. Graph this on your number line in part h. Does it fall in the rejection region(s)? (10 points).

1l. Do you reject  $H_0$  or not? (3 points).

1m. What do the results indicate regarding the relationship between sleep loss and the ability to maintain sustained attention. (4 points).

- 2 A store manager wants to determine if newspaper advertising really does affect sales. He randomly selects 10 items currently in stock and proceeds to establish a baseline by counting the number of each item sold over a 1-week period. Then, without changing the price of the items, he places a large ad in the newspaper, advertising the 10 items. Again, he counts the number of each item sold over a 1-week period. The number of items sold over the two 1-week periods are listed below:

Item #	Number sold before the ad	Number sold after the ad
1	25	32
2	18	24
3	3	7
4	16	18
5	20	25
6	23	20
7	10	15
8	25	23
9	32	34
10	15	15

a. State the scientific hypothesis and the PCH (plausible competing hypothesis) of chance (5 points).

b. Is the scientific hypothesis directional or nondirectional? Why? (2 points).

c. Name the test statistic you will use to decide between the statistical hypotheses (5 points).

- d. Translate the scientific hypothesis and the PCH of chance to statistical hypotheses – that is state  $H_0$  and  $H_1$  (2 points).
- e. What is the alpha level (level of significance or p-value) you will use? (2 points).
- f. In your own words, what does the alpha level mean? (3 points).
- g. Calculate the degrees of freedom (df) you will use for your critical value (or values) (4 points).
- h. What is the critical value (or values)? (2 points).
- i. Draw a line representing the range of your statistic. What is the value predicted by  $H_0$ ? Draw it on the line. Also draw the critical value (or values) on the line. Label the “Reject  $H_0$ ” region (or regions). Label the “Do not Reject  $H_0$ ” region. (5 points).
- j. Does the pattern of the data fit the scientific hypothesis? Why or why not? (2 points).
- k. Calculate the value of your test statistic from the data. Graph this on your number line in part i. Does it fall in the rejection region(s)? (10 points).
- l. Do you reject  $H_0$  or not? (3 points).
- m. What do the results indicate regarding the relationship between advertising and product sales. (4 points).

<b>t-table</b>						
	<b>one-tailed</b>	<b>0.05</b>	<b>0.025</b>	<b>0.01</b>	<b>0.005</b>	<b>0.001</b>
	<b>two-tailed</b>	<b>0.1</b>	<b>0.05</b>	<b>0.02</b>	<b>0.01</b>	<b>0.002</b>
<b>df</b>						
<b>1</b>		6.314	12.706	31.821	63.657	318.310
<b>2</b>		2.920	4.303	6.965	9.925	22.326
<b>3</b>		2.353	3.182	4.541	5.841	10.213
<b>4</b>		2.132	2.776	3.747	4.604	7.173
<b>5</b>		2.015	2.571	3.365	4.032	5.893
<b>6</b>		1.943	2.447	3.143	3.707	5.208
<b>7</b>		1.895	2.365	2.998	3.499	4.785
<b>8</b>		1.86	2.306	2.896	3.355	4.501
<b>9</b>		1.833	2.262	2.821	3.250	4.297
<b>10</b>		1.812	2.228	2.764	3.169	4.144
<b>11</b>		1.796	2.201	2.718	3.106	4.025
<b>12</b>		1.782	2.179	2.681	3.055	3.930
<b>13</b>		1.771	2.160	2.650	3.012	3.852
<b>14</b>		1.761	2.145	2.624	2.977	3.787
<b>15</b>		1.753	2.131	2.602	2.947	3.733
<b>16</b>		1.746	2.120	2.583	2.921	3.686
<b>17</b>		1.74	2.110	2.567	2.898	3.646
<b>18</b>		1.734	2.101	2.552	2.878	3.610
<b>19</b>		1.729	2.093	2.539	2.861	3.579
<b>20</b>		1.725	2.086	2.528	2.845	3.552
<b>21</b>		1.721	2.080	2.518	2.831	3.527
<b>22</b>		1.717	2.074	2.508	2.819	3.505
<b>23</b>		1.714	2.069	2.500	2.807	3.485
<b>24</b>		1.711	2.064	2.492	2.797	3.467
<b>25</b>		1.708	2.060	2.485	2.787	3.450
<b>26</b>		1.706	2.056	2.479	2.779	3.435
<b>27</b>		1.703	2.052	2.473	2.771	3.421
<b>28</b>		1.701	2.048	2.467	2.763	3.408
<b>29</b>		1.699	2.045	2.462	2.756	3.396
<b>30</b>		1.697	2.042	2.457	2.750	3.385
<b>40</b>		1.684	2.021	2.423	2.704	3.307
<b>60</b>		1.671	2.000	2.390	2.660	3.232
<b>120</b>		1.658	1.980	2.358	2.617	3.160
<b>inf</b>		1.645	1.960	2.326	2.576	3.090

Chi-squared table

	<b>one-tailed</b>	<b>0.050</b>	<b>0.010</b>	<b>0.001</b>
<b>df</b>				
1		3.84146	6.63490	10.828
2		5.99147	9.21034	13.816
3		7.81473	11.3449	16.266
4		9.48773	13.2767	18.467
5		11.0705	15.0863	20.515
6		12.5916	16.8119	22.458
7		14.0671	18.4753	24.322
8		15.5073	20.0902	26.125
9		16.9190	21.6660	27.877
10		18.3070	23.2093	29.588
11		19.6751	24.7250	31.264
12		21.0261	26.2170	32.909
13		22.3621	27.6883	34.528
14		23.6848	29.1413	36.123
15		24.9958	30.5779	37.697
16		26.2962	31.9999	39.252
17		27.5871	33.4087	40.790
18		28.8693	34.8053	42.312
19		30.1435	36.1908	43.820
20		31.4104	37.5662	45.315
21		32.6705	38.9321	46.797
22		33.9244	40.2894	48.268
23		35.1725	41.6384	49.728
24		36.4151	42.9798	51.179
25		37.6525	44.3141	52.620
26		38.8852	45.6417	54.052
27		40.1133	46.9630	55.476
28		41.3372	48.2782	56.892
29		42.5569	49.5879	58.302
30		43.7729	50.8922	59.703
40		55.7585	63.6907	73.402
50		67.5048	76.1539	86.661
60		79.0819	88.3794	99.607
70		90.5312	100.425	112.317
80		101.879	112.329	124.839
90		113.145	124.116	137.208
100		124.342	135.807	149.449

**F  
table**

**alpha  
=.05**

	<i>df upper</i>	1	2	3	4	5	6	7	8	9	10	12	15	20	24	30	40	60	120	inf
<i>df lower</i>																				
<b>1</b>		161.4	199.5	215.7	224.6	230.2	234.0	236.8	238.9	240.5	241.9	243.9	245.9	248.0	249.1	250.1	251.1	252.2	253.3	254.3
<b>2</b>		18.51	19.00	19.16	19.25	19.30	19.33	19.35	19.37	19.38	19.40	19.41	19.42	19.43	19.44	19.44	19.45	19.45	19.46	19.50
<b>3</b>		10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81	8.79	8.74	8.70	8.66	8.64	8.62	8.59	8.57	8.55	8.53
<b>4</b>		7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00	5.96	5.91	5.86	5.80	5.77	5.75	5.72	5.69	5.66	5.63
<b>5</b>		6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77	4.74	4.68	4.62	4.56	4.53	4.50	4.46	4.43	4.40	4.36
<b>6</b>		5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06	4.00	3.94	3.87	3.84	3.81	3.77	3.74	3.70	3.67
<b>7</b>		5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	3.64	3.57	3.51	3.44	3.41	3.38	3.34	3.30	3.27	3.23
<b>8</b>		5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39	3.35	3.28	3.22	3.15	3.12	3.08	3.04	3.01	2.97	2.93
<b>9</b>		5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.14	3.07	3.01	2.94	2.90	2.86	2.83	2.79	2.75	2.71
<b>10</b>		4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	2.98	2.91	2.85	2.77	2.74	2.70	2.66	2.62	2.58	2.54
<b>11</b>		4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	2.85	2.79	2.72	2.65	2.61	2.57	2.53	2.49	2.45	2.40
<b>12</b>		4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80	2.75	2.69	2.62	2.54	2.51	2.47	2.43	2.38	2.34	2.30
<b>13</b>		4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71	2.67	2.60	2.53	2.46	2.42	2.38	2.34	2.30	2.25	2.21
<b>14</b>		4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65	2.60	2.53	2.46	2.39	2.35	2.31	2.27	2.22	2.18	2.13
<b>15</b>		4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59	2.54	2.48	2.40	2.33	2.29	2.25	2.20	2.16	2.11	2.07

<b>16</b>	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54	2.49	2.42	2.35	2.28	2.24	2.19	2.15	2.11	2.06	2.01
<b>17</b>	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49	2.45	2.38	2.31	2.23	2.19	2.15	2.10	2.06	2.01	1.96
<b>18</b>	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46	2.41	2.34	2.27	2.19	2.15	2.11	2.06	2.02	1.97	1.92
<b>19</b>	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42	2.38	2.31	2.23	2.16	2.11	2.07	2.03	1.98	1.93	1.88
<b>20</b>	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39	2.35	2.28	2.20	2.12	2.08	2.04	1.99	1.95	1.90	1.84
<b>21</b>	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37	2.32	2.25	2.18	2.10	2.05	2.01	1.96	1.92	1.87	1.81
<b>22</b>	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34	2.30	2.23	2.15	2.07	2.03	1.98	1.94	1.89	1.84	1.78
<b>23</b>	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32	2.27	2.20	2.13	2.05	2.01	1.96	1.91	1.86	1.81	1.76
<b>24</b>	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30	2.25	2.18	2.11	2.03	1.98	1.94	1.89	1.84	1.79	1.73
<b>25</b>	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.28	2.24	2.16	2.09	2.01	1.96	1.92	1.87	1.82	1.77	1.71
<b>26</b>	4.23	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.27	2.22	2.15	2.07	1.99	1.95	1.90	1.85	1.80	1.75	1.69
<b>27</b>	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.25	2.20	2.13	2.06	1.97	1.93	1.88	1.84	1.79	1.73	1.67
<b>28</b>	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.24	2.19	2.12	2.04	1.96	1.91	1.87	1.82	1.77	1.71	1.65
<b>29</b>	4.18	3.33	2.93	2.70	2.55	2.43	2.35	2.28	2.22	2.18	2.10	2.03	1.94	1.90	1.85	1.81	1.75	1.70	1.64
<b>30</b>	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21	2.16	2.09	2.01	1.93	1.89	1.84	1.79	1.74	1.68	1.62
<b>40</b>	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12	2.08	2.00	1.92	1.84	1.79	1.74	1.69	1.64	1.58	1.51
<b>60</b>	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04	1.99	1.92	1.84	1.75	1.70	1.65	1.59	1.53	1.47	1.39
<b>120</b>	3.92	3.07	2.68	2.45	2.29	2.17	2.09	2.02	1.96	1.91	1.83	1.75	1.66	1.61	1.55	1.50	1.43	1.35	1.25
<b>inf</b>	3.84	3.00	2.60	2.37	2.21	2.10	2.01	1.94	1.88	1.83	1.75	1.67	1.57	1.52	1.46	1.39	1.32	1.22	1.00

**END OF EXAM**

\* Remember, when checking your score, your answers will be graded based on your prior responses. For example, if you answered that Question 1 is directional, you will lose a few points, but all other answers will be graded assuming that this is correct.

# Final Form 1 answer key

## Psychology 3000-090 - Online Statistics

5pts 1 a The scientific hypothesis is that sleep loss effects ability to maintain sustained attention.  
The null of chance is that sleep loss has no effect on ability to maintain sustained attention or that any difference is due to chance alone

2pts b  $H_0 : E(\alpha_j) = 0$  for all  $j$   
 $H_1 : E(\alpha_j) \neq 0$  for some  $j$

5pts c One-way ANOVA for independent means

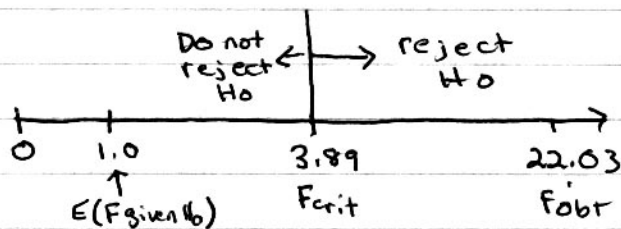
2pts d no

2pts e  $\alpha < .05$  OR  $P < .05$

4pts f  $df_{\text{B}} = J - 1 = 3 - 1 = 2$   
 $df_{\text{W}} = N - J = 15 - 3 = 12$

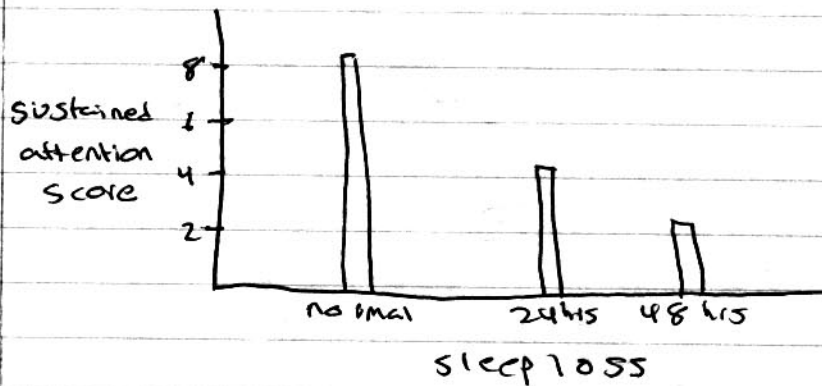
2pts g  $f_{\text{crit}}(2, 12)_{.05} = 3.89$

5pts h



Spts	i	Normal	24 hrs	48 hrs
		10	5	5
		9	4	2
		8	3	1
		7	4	2
		8	7	3
		$\Sigma X = 42$	23	13
		$\bar{M}_X = 8.4$	4.6	2.6

$$\Sigma X_{ij} = 78$$



2 pts j Yes, subjects with normal sleep scored highest, followed by those who were sleep deprived for 24 hours, with those sleep deprived for 48 hours performing worst

$$\begin{aligned}
 10 \text{ pts } k \text{ SSBE} &= \sum_j \left[ \frac{(\sum_i X_{ij})^2}{n_j} \right] - \frac{(\sum_j \sum_i X_{ij})^2}{N} \\
 &= \left[ \frac{42^2}{5} + \frac{23^2}{5} + \frac{13^2}{5} \right] - \frac{78^2}{15} \\
 &= \frac{2462}{5} - \frac{6084}{15} \\
 &= 492.4 - 405.6 \\
 &= 86.8
 \end{aligned}$$

$$SS_{WG} = \sum_j \sum_i X_{ij}^2 - \left[ \frac{(\sum_i X_{ij})^2}{n_j} \right]$$

NS	$x^2$	24 hrs	$x^2$	48 hrs	$x^2$
10	100	5	25	5	25
9	81	4	16	2	4
8	64	3	9	1	1
7	49	4	16	2	4
<u>8</u>	<u>64</u>	<u>7</u>	<u>49</u>	<u>3</u>	<u>9</u>
	358		115		43

$$\text{Total } X^2 = 516$$

$$SS_{WG} = 516 - 492.4 = 23.6$$

$$MS_{BG} = \frac{SS_{BG}}{df_{BG}} = \frac{86.8}{2} = 43.4$$

$$MS_{WG} = \frac{SS_{WG}}{df_{WG}} = \frac{23.6}{12} = 1.97$$

$$F = \frac{MS_{BG}}{MS_{WG}} = \frac{43.4}{1.97} = 22.03$$

F falls within the rejection region

3 pts L. Reject  $H_0$

4 pts m. This suggests that the relationship between sleep loss and performance on a sustained attention task is not due to chance alone.

5 pts 2 a. The scientific hypothesis is that newspaper advertising affects sales

The PCH of chance is that newspaper advertising has no affect on sales or that any change is due to chance alone.

2 pts b. nondirectional.

5 pts c. t-correlated

2 pts d.  $H_0: E(M_D) = 0$   
 $H_1: E(M_D) \neq 0$

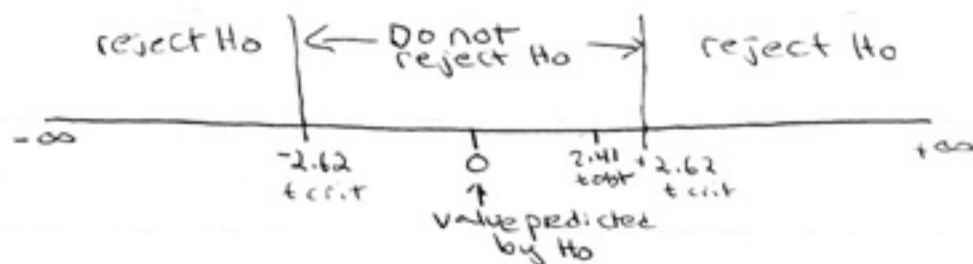
2 pts e.  $\alpha < .05$  or  $p < .05$

3 pts f. The acceptable probability level that the observed difference is due to sampling error or chance

4 pts g.  $df = N - 1 = 10 - 1 = 9$

2 pts h.  $t_{crit} = \pm 2.62$

5 pts i.



2 pts j. Yes, the data pattern fits the scientific hypothesis. Sales are higher after advertising than before.

10 pts k.

	before ad	after ad	difference (after-before)	$d^2$
1	25	32	7	49
2	18	24	6	36
3	3	7	4	16
4	16	18	2	4
5	20	25	5	25
6	23	20	-3	9
7	10	15	5	25
8	25	23	-2	4
9	32	34	2	4
10	15	15	0	0
			<hr/>	<hr/>
			26	172

$$M_d = 26/10 = 2.6$$

$$s_d = \sqrt{\frac{\sum d^2}{n_d} - (M_d)^2}$$

$$= \sqrt{\frac{172}{10} - (2.6)^2}$$

$$= \sqrt{17.2 - 6.76}$$

$$= \sqrt{10.44}$$

$$= 3.231$$

$$t = \frac{M_d}{s_d / \sqrt{n_d - 1}}$$

$$= \frac{2.6}{3.231 / \sqrt{10-1}}$$

$$= \frac{2.6}{3.231 / 3}$$

$$= \frac{2.6}{1.077}$$

$$= 2.41$$

Do not  
reject  $H_0$

3 pts L do not reject  $H_0$

4 pts m. The results indicate that the difference between sales before and after advertising could be explained by chance alone.